

# Extraordinary Optical Transmission Property of X-Shaped Plasmonic Nanohole Arrays

Yongkai Wang · Yan Qin · Zhongyue Zhang

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**Abstract** Optical transmission properties of periodic X-shaped plasmonic nanohole arrays in a silver film are investigated by performing the finite element method. Obvious peaks appear in the transmission spectra due to surface plasmon polaritons (SPPs) on the top surface of the silver film, to the Fabry–Férot resonance effect of SPPs in the nanohole, and to the localized surface plasmon resonance of the nanohole. Besides the topologic shape parameters of the X-shaped nanohole, transmission properties strongly depend on incident polarization. The results of this study not only present a tunable plasmonic filter, but also aid in the understanding of the mechanisms of the extraordinary optical transmission phenomenon.

**Keywords** Extraordinary optical transmission · Plasmonics · Surface plasmon polariton · Localized surface plasmon

## Introduction

In 1998, T. W. Ebbesen first studied the optical transmission properties of a periodic subwavelength rectangular hole in a thin metal film and found that light transmission rate is higher than the area ratio of the hole and the film when the aperture is smaller than the incident wavelength. This phenomenon is called extraordinary optical transmission (EOT) [1]. Given the association of the EOT phenomenon with integrated optics [2], highly sensitive biological sensing and detection [3],

surface-enhanced Raman scattering [4], and other nonlinear optical effects, EOT in a metal film with holes has gradually become popular topic for research [5–15].

EOT phenomenon is mainly due to the match between the wavelength of surface plasmon polaritons (SPPs) and the period of the aperture array [16]. For the subwavelength hole array inside a metallic film, when the array period matches the wavelength of SPPs excited on the film, strong electron oscillation is excited around the hole. The formed strong electron oscillation between two sides of the hole results in the larger transmittance funneled through the smaller aperture and propagate to the other side of the film. Thus, the localized surface plasmon (LSP) of the subwavelength hole also plays an important role in the EOT phenomenon [17–19]. To better understand the contribution of SPPs and of LSPs to the EOT phenomenon, researchers had fixed the shape and the size of hole and changed the period of the structure [20]. Previous results showed that both LSP and SPP have important roles in the EOT phenomenon and that when they exhibit a similar energy, the hole becomes conductive to transmission. In addition, the hole can be regarded as a Fabry–Férot resonant nanocavity, with both ends open. When the spread of SPPs in the hole satisfies a certain phase condition, the hole achieves maximum transmittance [21]. Hence, the length of the hole influences EOT.

Recently, researchers have investigated the optical transmission properties of nanoholes with circular [22], spheroid [23], and triangular [24] structures. When the shapes of the nanohole become more complex, novel transmission properties emerge [25–32].

In this paper, we examine optical transmission properties of X-shaped plasmonic nanohole arrays in a silver (Ag) film. Obvious peaks appear in the transmission spectra due to SPPs on the top surface of the film, to the Fabry–Férot resonance of SPPs in the nanohole, and to LSPs in the nanohole. In addition, we study the effect of topologic shape parameters of the

Y. Wang · Z. Zhang (✉)  
School of Physics and Information Technology, Shaanxi Normal University, Xi'an 710062, China  
e-mail: zyzhang@snnu.edu.cn

Y. Qin · Z. Zhang  
School of Physical Science and Technology, Southwest University, Chongqing 400715, China

X-shaped nanohole and of incident polarization to transmission properties.

### Structure and Computational Method

The X-shaped nanohole arrays analyzed in this study are presented in Fig. 1a. The nanoholes are arranged in a rectangular manner in the Ag film. The transverse and the longitudinal periods are  $a$  and  $b$ , respectively. The thickness of the Ag film is denoted as  $d$ . Figure 1b shows the enlarged X-shaped nanohole that has a width of  $w$  and a length of 300 nm. The inclined angle of the X-shaped nanohole is fixed at  $60^\circ$ . In the calculations, light irradiates perpendicularly to the film with a polarization angle  $\theta$  toward the  $x$ -direction, as shown in Fig. 1a. The transmission properties of the X-shaped nanohole arrays are numerically investigated by performing the finite element method (COMSOL Multiphysics). The complex relative permittivity of Ag is obtained from [33].

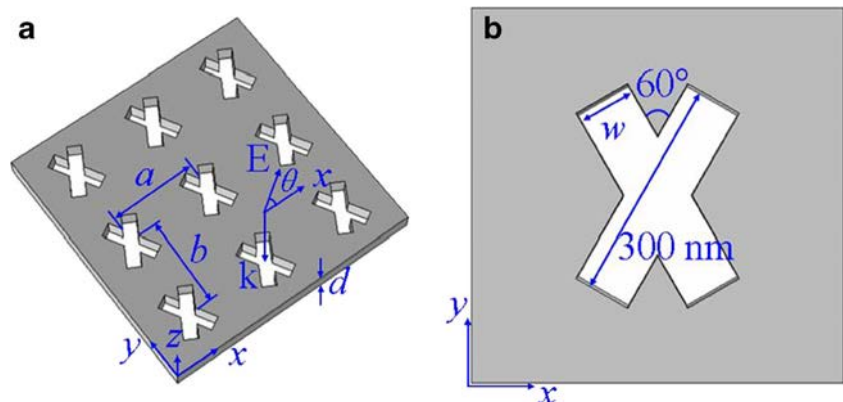
### Results and Discussion

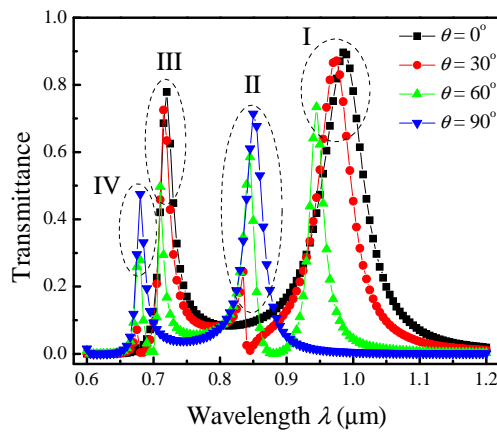
Figure 2 plots the simulated transmission spectra of the X-shaped nanohole arrays with different polarization angles  $\theta$  of  $0^\circ$ ,  $30^\circ$ ,  $60^\circ$ , and  $90^\circ$  with fixed  $a=500$  nm,  $b=500$  nm,  $d=200$  nm, and  $w=50$  nm. The wavelength of the spectrum ranges from 0.6 to 1.2  $\mu\text{m}$ . When  $\theta=0^\circ$ , two transmission peaks occur at  $\lambda=0.720$   $\mu\text{m}$  and  $\lambda=0.985$   $\mu\text{m}$ , respectively. When  $\theta=30^\circ$ , four transmission peaks appear at  $\lambda=0.675$   $\mu\text{m}$ ,  $\lambda=0.715$   $\mu\text{m}$ ,  $\lambda=0.835$   $\mu\text{m}$ , and  $\lambda=0.975$   $\mu\text{m}$ , respectively. With the increase in  $\theta$ , transmittances at  $\lambda=0.675$   $\mu\text{m}$  and  $\lambda=0.835$   $\mu\text{m}$  increase dramatically. Meanwhile, transmittances at  $\lambda=0.715$   $\mu\text{m}$  and  $\lambda=0.975$   $\mu\text{m}$  decrease. At  $\theta=90^\circ$ , transmittance peaks at approximately  $\lambda=0.715$   $\mu\text{m}$  and that at  $\lambda=0.975$   $\mu\text{m}$  disappear, and there are only two peaks in the transmission spectrum. Based on the trends demonstrated by the transmission peaks, we divide the

transmission peaks into four groups (modes I, II, III, and IV), as illustrated in Fig. 2.

To investigate the origins of the transmission peaks in Fig. 2, we examined the corresponding steady-state electric field distributions. Figure 3 shows the steady-state electric field distributions of the X-shaped nanohole at  $\theta=60^\circ$ . a, d, g, and j of Fig. 3 present the electric field distributions on the top surface of the film, and b, e, h, and k exhibit the electric field distributions at the cross sections of the  $zx$  plane through the center of the X-shaped nanohole. Lastly, c, f, i, and l of Fig. 3 display the electric field distributions at the cross sections of the  $yz$  plane through the center of the X-shaped nanohole. Given that the inclined angle of the X-shaped nanohole in the  $x$ -direction is  $60^\circ$ , the width of the hole in the  $x$ -direction is smaller than that in the  $y$ -direction. a to c in Fig. 3 demonstrates the steady-state electric field distributions at mode I ( $\lambda=0.945$   $\mu\text{m}$ ); in a of Fig. 3, electric field distributions strongly occur around the corners in the  $x$ -direction. A comparison between b and c of Fig. 3 shows that electric field distributions are stronger at the opposite sides of the X-shaped nanohole in the  $x$ -direction. Therefore, mode I can be attributed to LSP resonance of the X-shaped nanohole with the incident polarization component in the  $x$ -direction. Similarly, mode II is attributed to LSP resonance of the X-shaped nanohole with the incident polarization component in the  $y$ -direction. As shown in g to i of Fig. 3, at mode III ( $\lambda=0.710$   $\mu\text{m}$ ), electric field distributions strongly occur around the corners of the X-shaped nanohole in the  $x$ -direction, similar with that in a. However, at the cross sections of the  $zx$  and  $yz$  planes, electric field distributions strongly occur at the top and at the bottom surfaces of the nanohole, which are in contrast to those presented in b and c of Fig. 3, respectively. Mode III can be attributed to the resonance of SPPs in the nanohole at incident polarization in the  $x$ -direction. Similarly, mode IV is attributed to the resonance of SPPs in the nanohole at incident polarization in the  $y$ -direction. Therefore, the origins of modes I, II, III, and IV sufficiently interpret the polarization-dependent transmission spectra of the X-shaped nanohole arrays.

**Fig. 1** a The proposed X-shaped nanohole arrays and the irradiation condition. b Structural parameters of the X-shaped nanohole

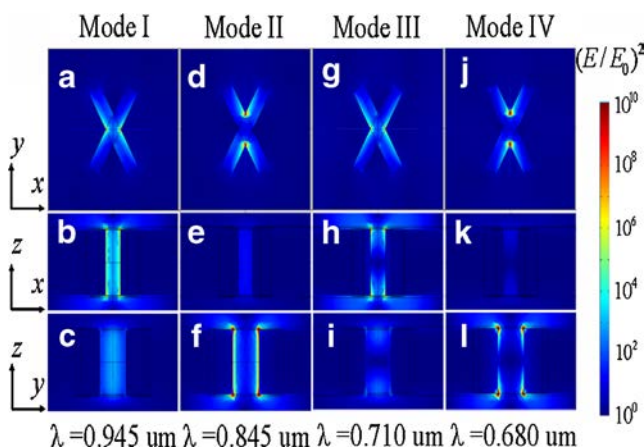




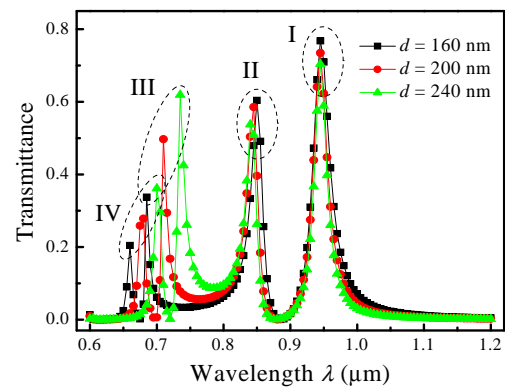
**Fig. 2** Calculated transmission spectra of the X-shaped nanohole arrays with different incident polarization angles

To investigate the effect of film thickness  $d$  on the transmittance of the X-shaped nanohole arrays,  $d$  is increased from  $d=160$  nm to  $d=240$  nm, with fixed  $a=500$  nm,  $b=500$  nm,  $w=50$  nm, and  $\theta=60^\circ$ . As shown in Fig. 4, modes I and II are weakly affected by  $d$ . However, the wavelengths of modes III and IV red shift dramatically as  $d$  increases. Given that modes I and II are attributed to LSP in the X-shaped nanohole at different incident polarizations, the increase of  $d$  does not affect LSP. Consequently, transmission peaks do not significantly shift. Given that modes III and IV are attributed to the resonance of SPPs in the nanohole, the increase of  $d$  increases the length of the resonator, resulting in the red shift of the resonant wavelengths.

To investigate the influence of the width  $w$  of the X-shaped nanohole on the transmittance spectra,  $w$  is increased from  $w=40$  nm to  $w=70$  nm, with fixed  $a=500$  nm,  $b=500$  nm,  $d=200$  nm, and  $\theta=60^\circ$ . As shown in Fig. 5, the wavelengths of modes I, II, III, and IV blue shift as  $w$  increases. Specifically, modes I and II blue shift dramatically from  $\lambda=0.985$   $\mu\text{m}$  to  $\lambda=0.920$   $\mu\text{m}$ , and from  $\lambda=0.905$   $\mu\text{m}$  to  $\lambda=0.800$   $\mu\text{m}$ , respectively. However, the wavelengths of modes III and IV



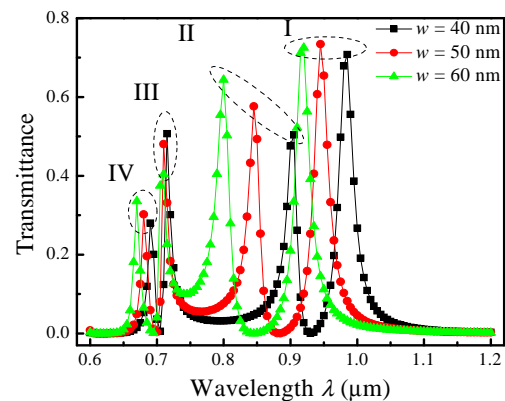
**Fig. 3** Steady-state electric field distributions of the X-shaped nanohole at modes I, II, III, and IV at  $\theta=60^\circ$



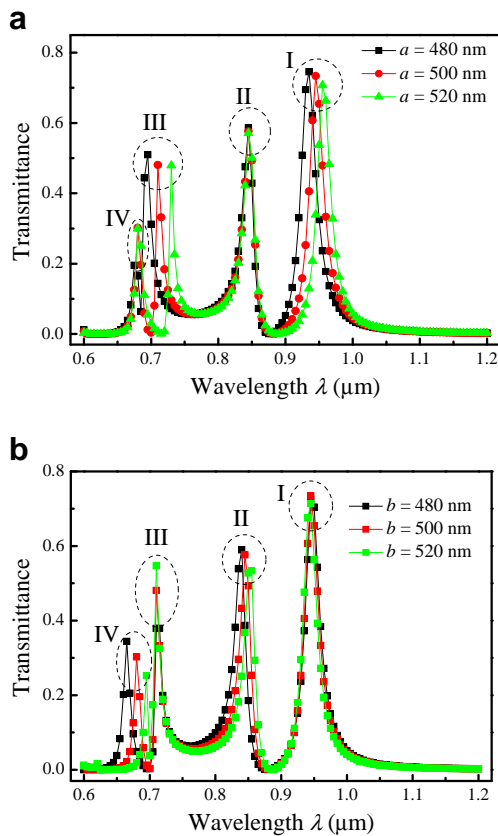
**Fig. 4** Calculated transmission spectra of the X-shaped nanohole arrays with different film thickness  $d$

do not significantly shift. As discussed previously, modes I and II are attributed to LSP in the X-shaped nanohole. Therefore, an increase in the width of the X-shaped nanohole will reduce the gap between adjacent nanoholes, resulting in the blue shift of the wavelengths of modes I and II. Meanwhile, an increase in  $w$  will decrease the confinement of SPPs in the nanohole, subsequently increasing the wavelength of SPPs in a one specific excitation wavelength. As a result, the resonant modes of modes III and IV blue shift. With the width at the cross section of the  $yz$  plane varying faster than that of the  $xz$  plane as  $w$  increases, the transmission peak of mode IV blue shifts faster than that of mode III.

To investigate the effect of the period to the transmittance spectra, we vary the periods of the X-shaped nanohole arrays in the  $x$ - and in the  $y$ -directions. Figure 6a shows the simulated transmittance spectra with different transverse periods  $a$  in the  $x$ -direction, with fixed  $b=500$  nm,  $d=200$  nm,  $w=50$  nm, and  $\theta=60^\circ$ . Four transmission peaks are observed in the spectra, corresponding to modes I, II, III, and IV. The wavelengths of modes II and IV do not noticeably shift because they correspond to the incident polarization in the  $y$ -direction. In contrast, modes I and III are much more sensitive to the period in the  $x$ -direction. An increase in the



**Fig. 5** Calculated transmission spectra of the X-shaped nanohole arrays with different slit width  $w$



**Fig. 6** Calculated transmission spectra of the X-shaped nanohole arrays with **a** different periods in the  $x$ -direction and **b** different periods in the  $y$ -direction

transverse period of the X-shaped nanohole by 20 nm results in a red shift of the transmittance peaks by approximately 20 and 40 nm, respectively. Given that mode I is attributed to LSP resonance of the X-shaped nanohole, the increase in  $a$  will increase the electron oscillation length on the metal film, resulting in the red shift of the wavelength of mode I. At mode III, SPPs on the top surface are coupled into the nanohole. To achieve maximum transmittance, the period of the nanohole should match the wavelength of SPPs on the top surface of the Ag film. Thus, the wavelengths of mode III red shift as  $a$  increases. Figure 6b shows the simulated transmittance spectra with different longitudinal periods  $b$  in  $y$ -direction, with fixed  $a=500$  nm,  $d=200$  nm,  $w=50$  nm, and  $\theta=60^\circ$ . Four obvious transmission peaks appear in the spectra. The wavelengths of modes I and III do not shift as  $b$  increases. However, the wavelengths of modes II and IV red shift as  $b$  increases. These trends are similarly explained with those exhibited in Fig. 6a.

## Conclusion

In this paper, transmission properties of periodic X-shaped plasmonic nanohole arrays are studied numerically. Results

show that four transmission peaks occur in the transmission spectra of the nanohole arrays due to SPPs on the top surface of the Ag film, to the resonance effect of SPPs in the nanohole, and to LSP in the nanohole. Given that the X-shaped nanohole is anisotropic, its transmission properties are strongly dependent on incident polarizations. In addition, the structural parameters of the X-shaped nanohole and the nanohole array periods strongly affect transmission properties. The results of this study will not only be significant for specific plasmonic applications, but will also be helpful in understanding the mechanisms of the EOT phenomenon.

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